

# FINAL ANSWER KEY

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Question1:-Who wrote the book namely 'Kristhu sahasra namam' ?

- A:-Pambadi John Joseph
- B:-Chattampi Swamikal
- C:-C. Kesavan
- D:-Chavara Kuriakkose Elias Achan

Correct Answer:- Option-C

Question2:-Silvassa is the capital city of

- A:-Daman and Diu
- B:-Puducherry
- C:-Dadra Nagar Haveli
- D:-Mizoram

Correct Answer:- Option-C

Question3:-Brian Acton and Jan Koum are the founders of popular mobile app namely

- A:-WhatsApp
- B:-Instagram
- C:-Google
- D:-Google chrome

Correct Answer:- Option-A

Question4:-Who among the following was the leader of 'Rajadhani March' of 1939 ?

- A:-Akkamma Cheriyan
- B:-T.M. Varghese
- C:-Vakkam Abdulkhadar Maulavi
- D:-A.K. Gopalan

Correct Answer:- Option-A

Question5:-'Chenthuruni' wildlife sanctuary is in \_\_\_\_\_ district of Kerala.

- A:-Idukky
- B:-Pathanamthitta
- C:-Kollam
- D:-Ernakulam

Correct Answer:- Option-C

Question6:-Which was the main centre of Kallumala Samaram of 1915 led by Ayyankali ?

- A:-Venganoor
- B:-Perinad
- C:-Panmana
- D:-Vanchiyoor

Correct Answer:- Option-B

Question7:-'Yudh Abhyas 2016' is the joint military training exercise between India and

- A:-France
- B:-Japan
- C:-Korea
- D:-USA

Correct Answer:- Option-D

Question8:-'Changampuzha; Nakshathrangalude Snehabhajanam' is the book written by

- A:-K.P. Appan
- B:-M.K. Sanu
- C:-M. Leelavathi
- D:-N. Krishnapillai

Correct Answer:- Option-B

Question9:-'Oneirology' is the study of

- A:-Dreams
- B:-Beauty of human
- C:-Birds
- D:-Fashion

Correct Answer:- Option-A

Question10:-'Thiruvithamkoor Rashtreeya Mahasabha' was founded under the leadership of

- A:-Dr. Velukkutty Arayan
- B:-T.K. Madhavan
- C:-Pandit Karuppan
- D:-G.P. Pillai

Correct Answer:- Option-A

Question11:-'He who has a taste for every sort of knowledge and who is curious to learn and is never satisfied may be justly termed a philosopher', was quoted by

- A:-Rousseau in 'Emile'
- B:-John Dewey in 'Freedom and Culture'
- C:-Plato in 'The Republic'
- D:-Aristotle in 'Aristotle on Education'

Correct Answer:- Option-C

Question12:-Role playing is developed by using

- A:-Micro teaching
- B:-Simulation technique
- C:-Interaction analysis
- D:-All the above

Correct Answer:- Option-B

Question13:-Anecdotal record techniques is used in

- A:-Measurement
- B:-Evaluation
- C:-Examinations
- D:-None of these

Correct Answer:- Option-B

Question14:-Good teachers are known not for the fund of knowledge they possess but for their

- A:-Astute sense of wit and wisdom
- B:-Awe-inspiring personality
- C:-Warm and close relationship with their students
- D:-Enviably teaching methodology

Correct Answer:- Option-D

Question15:-To raise the standard of education, it is necessary

- A:-To evaluate students continuously
- B:-To give high salary to teachers
- C:-To revise curriculum
- D:-To make good school building

Correct Answer:- Option-A

Question16:-A survey design that collects consensus opinions of Panel of experts and the judgement is known as

- A:-Historical method
- B:-Case study method
- C:-Delphi technique
- D:-Interview method

Correct Answer:- Option-C

Question17:-If you find someone else publishes work similar to yours before your project is completed, what could you do ?

- A:-There is nothing you can do so do not mention it in your study
- B:-Completely revamp your ideas so you are not replicating it in your study
- C:-Acknowledge it in your report and evaluate the study
- D:-Present report after making some changes in your hypothesis and aims

Correct Answer:- Option-C

Question18:-A technique of building up a list or a sample of a special population by using an initial set of members as informants is called

- A:-Quota sampling
- B:-Snowball sampling
- C:-Convenience sampling

D:-Purposive sampling

Correct Answer:- Option-B

Question19:-From research viewpoint seminars, conferences, symposia, workshops etc. whether national or international are the finest forums for

A:-Scientific interaction among professionals

B:-Social interaction among like-minded individuals

C:-Gathering latest knowledge on a research problem

D:-Locating, research problems in a field of knowledge

Correct Answer:- Option-D

Question20:-The methods of statistics which is used to derive conclusion about the characteristics of the whole with the help of data is called

A:-Derivative statistics

B:-Descriptive statistics

C:-Narrative statistics

D:-None of them

Correct Answer:- Option-A

Question21:-Which article of the constitution is known as necessary evil ?

A:-Article 17

B:-Article 15

C:-Article 32

D:-Article 22

Correct Answer:- Option-D

Question22:-Which amendment of the constitution lowered voting age from 21 to 18 ?

A:-` 42^(nd)`

B:-` 44^(th)`

C:-` 61^(st)`

D:-` 69^(th)`

Correct Answer:- Option-C

Question23:-When a constitution amendment bill is sent to the president of India, he

A:-has to sign it

B:-may return it for reconsideration

C:-may veto it

D:-may refer it to Supreme Court for advice

Correct Answer:- Option-A

Question24:-How can a member of the U.P.S.C. be removed from service ?

A:-only by the president of India

B:-only by impeachment

C:-on reaching the age of 60 (sixty)

D:-none of the above

Correct Answer:- Option-A

Question25:-Parliament can legislate in which of the following ?

A:-actionable wrongs

B:-bankruptcy and insolvency

C:-trust and trustees

D:-all of the above

Correct Answer:- Option-D

Question26:-Under prevention of children from Sexual Offences Act, child means

A:-a person under 18 years of age

B:-a person under 14 years of age

C:-a person under 16 years of age

D:-none of the above

Correct Answer:- Option-A

Question27:-According to sexual harassment of women at work place (prevention, prohibition and redressal) Act, 2013, for non compliance with the provisions of the Act, employer is liable to a fine of

A:-Rs. 20,000

B:-Rs. 50,000

C:-Rs. 1,00,000

D:-None of the above

Correct Answer:- Option-B

Question28:-In order to take organ for donation from a person who has under gone brain death

- A:-two certifications are required from any two doctors six hours apart
- B:-three certifications are required from three neurologists 4 hours apart
- C:-two certifications are required 6 hours apart from doctors nominated by government and two must be neurologists
- D:-none of the above

Correct Answer:- Option-C

Question29:-National Rural Employment Guarantee Act was passed in the year

- A:-2006
- B:-2007
- C:-2008
- D:-2005

Correct Answer:- Option-D

Question30:-Which among the following is a flow of polluter pay principle ?

- A:-there is ambiguity in determining who is a polluter
- B:-a large number of poor house holds, informal sector firms and subsistence farmers cannot bear any additional charges for waste disposal
- C:-small and medium size firms from formal sector, find it difficult to pass on higher costs to domestic end users of the product
- D:-all of the above

Correct Answer:- Option-D

Question31:-The complete bipartite graph  $K_{(7,5)}$  has

- A:-2 edges
- B:-12 edges
- C:-35 edges
- D:- $7^5$  edges

Correct Answer:- Option-C

Question32:-Area of the ellipse  $\frac{x^2}{25} + \frac{y^2}{16} = 1$  is

- A:- $20\pi$
- B:- $\frac{320}{3}\pi$
- C:- $\frac{400}{3}\pi$
- D:- $400\pi$

Correct Answer:- Option-A

Question33:-Perimeter of the cardioid  $r = 1 - \cos\theta$  is

- A:-1
- B:-2
- C:-4
- D:-8

Correct Answer:- Option-D

Question34:-Area of the surface generated by revolving the curve  $y = x$  about the x-axis from  $x = 0$  to  $x = 1$  is

- A:- $2\pi$
- B:- $2\sqrt{2}\pi$
- C:- $\sqrt{2}\pi$
- D:- $4\pi$

Correct Answer:- Option-B

Question35:-In Boolean algebra the law  $a + (a \cdot b) = a$  is known as

- A:-idempotent law
- B:-distributive law
- C:-boundedness law
- D:-absorption law

Correct Answer:- Option-D

Question36:-Transcendence of e was proved by

- A:-Euler
- B:-Cauchy
- C:-Euclid
- D:-Hermite

Correct Answer:- Option-D

Question37:-Which of the following is false ?

- A:- $2^{13} \equiv 1 \pmod{3}$
- B:- $3^{13} \equiv 1 \pmod{2}$
- C:- $13^2 \equiv 1 \pmod{3}$

D:  $13^3 \equiv 1 \pmod{2}$

Correct Answer: Option-A

Question38: Equation of the tangent to the circle  $x^2 + y^2 = 1$  at  $(\frac{1}{\sqrt{2}}, \frac{1}{\sqrt{2}})$  is

A:  $x + y = 1$

B:  $x + y = \frac{1}{\sqrt{2}}$

C:  $x + y = \sqrt{2}$

D:  $x - y = 1$

Correct Answer: Option-C

Question39: Degree of the field extension  $\mathbb{Q}(\sqrt{3} + \sqrt{2})$  over  $\mathbb{Q}(\sqrt{3})$  is

A: 1

B: 2

C: 3

D: 4

Correct Answer: Option-B

Question40: Number of subgroups of  $\mathbb{Z}_{18}$  is

A: 2

B: 3

C: 6

D: 18

Correct Answer: Option-C

Question41: Which of the following function  $f: \mathbb{R} \rightarrow \mathbb{R}$  is not a permutation?

A:  $f(x) = x + 1$

B:  $f(x) = x - 1$

C:  $f(x) = x^2 - 1$

D:  $f(x) = x^3 - 1$

Correct Answer: Option-C

Question42: Set of all integers  $\mathbb{Z}$  is

A: an integral domain but not a field

B: a division ring but not a field

C: a strictly skew field but not a field

D: a division ring but not an integral domain

Correct Answer: Option-A

Question43: Number of generators of  $\mathbb{Z}_{20}$  is

A: 1

B: 2

C: 4

D: 8

Correct Answer: Option-D

Question44: Let  $\mathbb{R}$  be the ring of real numbers. Units of  $\mathbb{R}$  are

A: 0

B: elements of  $\mathbb{R} \setminus \{0\}$

C: 1

D: elements of  $\mathbb{R} \setminus \{1\}$

Correct Answer: Option-B

Question45: Which of the following is false?

A: Every integral domain is a field

B: Every field is an integral domain

C: If  $p$  is a prime, then  $\mathbb{Z}_p$  is a field

D: Every finite integral domain is a field

Correct Answer: Option-A

Question46: The remainder of  $3^{50}$  when divided by 13 is

A: 6

B: 9

C: 3

D: 0

Correct Answer: Option-B

Question47:  $\prod_{n=1}^{\infty} \frac{(-1)^n}{(n)} \cdot \frac{1}{(n)} =$

A:  $[-1, 1]$

B:  $\{0\}$

C:  $\phi$

D: (0, 1)

Correct Answer: Option-B

Question48:  $\lim_{n \rightarrow \infty} (1 + (\log(e^2))/n)^n =$

A: -1

B: -2

C:  $e^2$

D:  $\log(e^2)$

Correct Answer: Option-B

Question49: Let  $g(x) = |\cos x|$ . Then

A:  $g(x)$  is nowhere differentiable

B:  $g(x)$  is everywhere differentiable

C:  $g(x)$  is differentiable everywhere except  $x = n\pi, n \in \mathbb{Z}$

D:  $g(x)$  is differentiable everywhere except  $x = (2n+1)\pi/2, n \in \mathbb{Z}$

Correct Answer: Option-D

Question50:

Let  $f(x) = \begin{cases} x^2 \sin \frac{1}{x}, & \text{if } x \neq 0 \\ 0, & \text{otherwise} \end{cases}$

Then :

A:  $f$  is differentiable at all points, but  $f'$  is not a continuous function

B:  $f$  is not differentiable but it is continuous

C:  $f$  is neither differentiable nor continuous

D:  $f$  is differentiable and  $f'$  is continuous

Correct Answer: Option-A

Question51:  $\int_0^{\infty} e^{-x^2} dx =$

A: -1

B:  $\pi/2$

C:  $\sqrt{\pi}/2$

D:  $\pi$

Correct Answer: Option-C

Question52: Bolzano-Weierstrass theorem

A: Every convergent sequence of real numbers is bounded

B: A bounded sequence of real numbers has a convergent subsequence

C: Every sequence of real numbers has a convergent subsequence

D: A sequence of non-negative real numbers is bounded if and only if it is convergent

Correct Answer: Option-B

Question53:  $\lim_{x \rightarrow 0} ((1 - \cos x) \sin x) / (x^2 + x^3) =$

A: -1

B: 0

C:  $1/2$

D: 1

Correct Answer: Option-C

Question54:  $i^{321} + (1/i^{123}) =$

A: 0

B: -2

C:  $-2i$

D:  $1 - i$

Correct Answer: Option-C

Question55:  $|z+3i| + |z-3i| = 8$  represents

A: a straight line

B: a circle

C: a hyperbola

D: an ellipse

Correct Answer: Option-D

Question56: Harmonic conjugate of  $u(x, y) = x^2 - y^2$  is

A:  $v(x, y) = x^2 + y^2$

B:  $v(x, y) = (x+y)^2$

C:  $v(x, y) = (x-y)^2$

D:  $v(x, y) = 2xy$

Correct Answer: Option-D

Question57: Let  $C$  be the positively oriented circle  $|z| = 4$ . Then  $\oint_C (z^2 dz)/(z-1) + \oint_C (z^2 dz)/(z-1)^2 =$

A:  $6\pi i$

B:  $2\pi i$

C:  $\pi i$

D: 0

Correct Answer: Option-A

Question58: If  $f(z)$  is continuous in a simply connected domain  $D$  and if  $\oint_C f(z) dz = 0$  for every closed path in  $D$ , then  $f(z)$  is analytic in  $D$

A: Liouville's theorem

B: Morera's theorem

C: Cauchy's integral theorem

D: Cauchy's integral formula

Correct Answer: Option-B

Question59: The radius of convergence of the power series  $\sum_{n=0}^{\infty} \frac{(2n)!}{(n!)^2} (z-2)^n$  is

A: 0

B:  $1/4$

C:  $1/2$

D:  $\infty$

Correct Answer: Option-B

Question60: At  $z = 0$ , the function  $f(z) = e^{(1/z)}$  has

A: a removable singularity

B: a simple pole

C: an essential singularity

D: no singular point

Correct Answer: Option-C

Question61: Let  $f(z) = (1 - \cos z)/(z^5)$ . Then  $f(z)$  has

A: a pole of order 3 and residue  $(-1)/(24)$  at  $z = 0$

B: a pole of order 5 and residue  $(-1)/(24)$  at  $z = 0$

C: a pole of order 3 and residue  $(1)/(5)$  at  $z = 0$

D: a pole of order 5 and residue  $(1)/(5)$  at  $z = 0$

Correct Answer: Option-A

$$\text{Res}_{z=3i} \frac{z+1}{z^2+9} =$$

Question62:

A:  $(3+i)/(6)$

B:  $(3-i)/(6)$

C:  $(1+3i)/(9)$

D:  $(1-3i)/(9)$

Correct Answer: Option-B

Question63: Which of the following is false?

A: Every order topology is Hausdorff

B: Subspace of a Hausdorff space is Hausdorff

C: Every Hausdorff space is normal

D: Product of two Hausdorff spaces is Hausdorff

Correct Answer: Option-C

Question64: Deleted comb space is

A: connected and path connected

B: connected but not path connected

C: not connected but path connected

D: neither connected nor path connected

Correct Answer: Option-B

Question65: Which of the following need not be a normal space?

A: product of two normal spaces

B: a metrizable space

C: a compact Hausdorff space

D: a regular space with a countable basis

Correct Answer: Option-A

Question66:-Which of the following is false ?

- A:-the one point compactification of the real line  $\mathbb{R}$  is homeomorphic to an ellipse
  - B:-the one point compactification of the open interval  $(0, 1)$  is homeomorphic to closed interval  $[0, 1]$
  - C:-the one point compactification of the open interval  $(0, 1)$  is homeomorphic to the circle  $S^1$
  - D:-the one point compactification of  $\mathbb{R}^2$  is homeomorphic to the sphere  $S^2$
- Correct Answer:- Option-B

Question67:-Which of the following is not a topological property ?

- A:-length and area
- B:-connectedness
- C:-continuity
- D:-compactness

Correct Answer:- Option-A

Question68:-Let  $d$  be a metric defined on  $\mathbb{R}$  by

$$d(a, b) = \begin{cases} 0, & \text{if } a = b \\ 1, & \text{if } a \neq b \end{cases}$$

Then

- A:- $d$  is a pseudo metric on  $\mathbb{R}$
- B:- $d$  is the usual metric on  $\mathbb{R}$
- C:- $d$  is the Euclidean metric on  $\mathbb{R}$
- D:- $d$  is the trivial metric on  $\mathbb{R}$

Correct Answer:- Option-D

Question69:-Which of the following is not a basis for  $\mathbb{R}^3$  ?

- A:-  $\{(1, 1, 1), (1, 1, 0), (1, 0, 0)\}$
- B:-  $\{(1, 1, 1), (0, 1, 1), (1, 0, 0)\}$
- C:-  $\{(1, 1, 1), (0, 1, 1), (0, 0, 1)\}$
- D:-  $\{(1, 0, 0), (0, 1, 0), (0, 0, 1)\}$

Correct Answer:- Option-B

Question70:-Let  $T : \mathbb{R}^3 \rightarrow \mathbb{R}^3$  be a map defined on  $\mathbb{R}^3$ . Then which of the following is not a linear transformation ?

- A:- $T(x, y, z) = (y, x, 0)$
- B:- $T(x, y, z) = (x + y, y + z, z + x)$
- C:- $T(x, y, z) = (xy, yz, xz)$
- D:- $T(x, y, z) = (0, 0, 0)$

Correct Answer:- Option-C

Question71:-Let  $P_5(x)$  be the set of all real polynomials of degree  $\leq 5$ . Then dimension of the vector space  $P_5(x)$  over  $\mathbb{R}$  is

- A:-0
- B:-1
- C:-5
- D:-6

Correct Answer:- Option-D

Question72:-Let  $T : \mathbb{R}^4 \rightarrow \mathbb{R}^5$  be defined by  $T(x_1, x_2, x_3, x_4) = (x_1, x_2, x_3, x_4, 0)$ . Then the dimension of the null space is

- A:-  $\dim(T) = 0$
- B:-  $\dim(T) = 1$
- C:-  $\dim(T) = 4$
- D:-  $\dim(T) = 5$

Correct Answer:- Option-A

Question73:-Characteristic polynomial of  $\begin{bmatrix} 1 & -1 & 0 \\ 0 & 1 & -1 \\ -1 & 0 & 1 \end{bmatrix}$  is

- A:-  $\lambda^3 + 3\lambda^2 + 3\lambda + 1 = 0$
- B:-  $\lambda^3 - 3\lambda^2 + 3\lambda - 1 = 0$
- C:-  $\lambda^3 - 3\lambda^2 + 3\lambda - 2 = 0$
- D:-  $\lambda^3 - 3\lambda^2 + 3\lambda = 0$

Correct Answer:- Option-D

Question74:-Let  $2x + y - z = 4$

$$\begin{aligned} x + 3y + 2z &= 1 \\ 3x + 4y + z &= 5 \end{aligned}$$

The above system of equation is

- A:-homogeneous and consistent

B:-nonhomogeneous and inconsistent

C:-consistent and has unique solution

D:-consistent and has infinite solution

Correct Answer:- Option-D

Question75:-Which of the following map  $T: \mathbb{R}^3 \rightarrow \mathbb{R}^3$  is a linear functional ?

A:-  $T(x,y,z)=5$

B:-  $T(x, y, z) = x^2$

C:-  $T(x,y,z)=-2x+y$

D:-  $T(x,y, z)=xy+6$

Correct Answer:- Option-C

Question76:-Let  $V$  be a vector of dimension 15 over a field  $F$  and  $W$  be a subspace of  $V$ . If  $\dim W = 3$ , then  $\dim(V/W)=$

A:-3

B:-5

C:-8

D:-12

Correct Answer:- Option-D

Question77:-An  $n \times n$  matrix is diagonalizable if

A:-all the eigen values are real and distinct

B:-all the eigen values are real and non-negative

C:-all the eigen values are real and non-zero

D:-all the eigen values are non-zero rational numbers

Correct Answer:- Option-A

Question78:-Let  $1 \leq p < \infty$  and let  $x \in L^p$  with  $\|x\|_p \leq 1$ . Then the inequality  $\|x\|_r \leq \|x\|_p$  is called

A:-Minkowski's inequality

B:-Jensen's inequality

C:-Cauchy's inequality

D:-Bessel's inequality

Correct Answer:- Option-B

Question79:-Which of the following is false ?

A:-  $L^p$  is a Hilbert space, where  $1 \leq p < \infty$

B:-Closed subspace of a Hilbert space is a Hilbert space

C:-The quotient of a Hilbert space by one of its closed subspace is again a Hilbert space

D:-A complete normed space with its norm satisfies the parallelogram law is a Hilbert space

Correct Answer:- Option-A

Question80:-Let  $A$  in  $BL(H)$  and  $A^*$  be the adjoint of  $A$ .  $A$  is unitary if

A:-  $AA^* = A^*A$

B:-  $AA^* \neq A^*A$

C:-  $A^* = A^{-1}$

D:-  $A^* = A$

Correct Answer:- Option-C

Question81:-Which of the following is not a Banach space ?

A:-Finite dimensional normed spaces

B:-  $L^p$  with norm  $\|\cdot\|_p$ , where  $1 \leq p < \infty$

C:-  $C_0$

D:-  $L^p(E)$  with the norm  $\|\cdot\|_p$ , where  $E$  is a Lebesgue measurable subset of  $\mathbb{R}$  and  $1 \leq p < \infty$

Correct Answer:- Option-C

Question82:-Let  $X$  be an inner product space and let  $x, y \in X$ . Then the parallelogram law is

A:-  $\|x+y\|^2 + \|x-y\|^2 = 2(\|x\|^2 + \|y\|^2)$

B:-  $\|x+y\|^2 + \|x-y\|^2 = \|x\|^2 + \|y\|^2$

C:-  $\|x+y\| \leq \|x+z\| + \|z+y\|$

D:-  $\sqrt{\|x\|^2 + \|y\|^2} \leq \|x+y\|$

Correct Answer:- Option-A

Question83:-Let  $X$  and  $Y$  be normed spaces and  $F: X \rightarrow Y$  be a linear map. The following conditions are equivalent except one. Which of the following is not equivalent to others ?

A:-  $F$  is continuous at 0

B:-  $F$  is continuous on  $X$

C:-  $a\|x\| \leq \|F(x)\|$ , for all  $x \in X$  and some  $a > 0$

D:-  $F$  is uniformly continuous on  $X$

Correct Answer:- Option-C

Question84:-If a, b, c are the roots of the equation  $x^3+px^2+qx+r=0$ , then  $1/a+1/b+1/c=$

A:-  $(-q)/(r)$

B:-  $(p)/(r)$

C:-  $(-p)/(r)$

D:-  $p/q$

Correct Answer:- Option-A

Question85:-The vector projection of  $\vec{B} = \hat{i} + \hat{j} + \hat{k}$  onto  $\vec{A} = 5\hat{j} - 3\hat{k}$  is

A:-  $\hat{i} + 6\hat{j} - 2\hat{k}$

B:-  $\hat{i} - 4\hat{j} + 4\hat{k}$

C:-  $\frac{1}{\sqrt{3}}(5\hat{j} - 3\hat{k})$

D:-  $\frac{1}{17}(5\hat{j} - 3\hat{k})$

Correct Answer:- Option-D

Question86:-  $\frac{d}{dx} \sinh^{-1}(x) =$

A:-  $\frac{1}{(\sqrt{1-x^2})}$

B:-  $\frac{1}{(\sqrt{1+x^2})}$

C:-  $\frac{1}{(\sqrt{x^2-1})}$

D:-  $\frac{1}{(1+x^2)}$

Correct Answer:- Option-B

Question87:-Equation of the tangent at the point  $(x_1, y_1)$  on the parabola  $y^2=4ax$  is

A:-  $yy_1=2a(x+x_1)$

B:-  $y-y_1=4a(x-x_1)$

C:-  $y=y_1/x_1(x-2a)$

D:-  $y = 2ax$

Correct Answer:- Option-A

Question88:-Rank of the matrix  $\begin{bmatrix} 3 & 4 & 1 \\ -2 & 3 & 2 \\ 5 & 1 & -1 \end{bmatrix}$  is

A:-0

B:-1

C:-2

D:-3

Correct Answer:- Option-C

Question89:-  $\lim_{(x,y) \rightarrow (0,0)} \frac{(5x^2y)}{(2x^4+y^2)} =$

A:-0

B:-  $5/3$

C:-  $5/2$

D:-limit does not exist

Correct Answer:- Option-D

Question90:-Let  $f(x)=x^3-12x+9$ . Then f(x) has a local maximum at

A:-  $x = 0$

B:-  $x = 3$

C:-  $x = 2$

D:-  $x = -2$

Correct Answer:- Option-D

Question91:-Let  $W=x^2+y^2$ ,  $x = r - S$  and  $y = r + S$ . Then the partial derivative of W with respect to S is

A:-  $(\partial W)/(\partial S)=1$

B:-  $(\partial W)/(\partial S)=2S$

C:-  $(\partial W)/(\partial S)=4S$

D:-  $(\partial W)/(\partial S)=2r$

Correct Answer:- Option-C

Question92:-Solution of the differential equation  $(d^2y)/(dx^2)-6dy/dx+13y=0$  is

A:-  $Ae^{3x}+Be^{2x}$

B:  $e^{(3x)}(\text{Acos}2x + \text{Bsin}2x)$

C:  $-\text{Acos}2x + \text{Bsin}2x$

D:  $-Ax^2 + Bx^3$

Correct Answer: Option-B

Question93: Solution of the equation  $(1+2xy+y^2)dx + (1+2xy+x^2)dy = 0$  is

A:  $x + x^2y + xy^2 + y = k$

B:  $x + 2x^2y + 2xy^2 + y = k$

C:  $4x + 4y = k$

D:  $1 + 2xy + x^2 + y^2 = k$

Correct Answer: Option-A

Question94: Let  $f(x) = \sum_{n=1}^{\infty} b_n \sin nx$  be the Fourier series of  $f(x) = x$  in the interval  $[-\pi, \pi]$ . Then  $b_n =$

A: 0

B:  $\frac{1}{n}$

C:  $\frac{(-1)^n}{n^2}$

D:  $\frac{2(-1)^{n+1}}{n}$

Correct Answer: Option-D

Question95: Laplace transform of  $e^{at} \sin bt$  is

A:  $\frac{s}{(s^2 + b^2)}$

B:  $\frac{s-a}{((s-a)^2 + b^2)}$

C:  $\frac{b}{((s-a)^2 + b^2)}$

D:  $\frac{b}{(s-a)^2 - b^2}$

Correct Answer: Option-C

Question96: Two dimensional Laplace equation is

A:  $\frac{\partial^2 u}{\partial x^2} = c^2 \frac{\partial^2 u}{\partial y^2}$

B:  $\frac{\partial^2 u}{\partial x^2} + \frac{\partial^2 u}{\partial y^2} = 0$

C:  $\frac{\partial^2 u}{\partial x^2} + \frac{\partial^2 u}{\partial y^2} = f(x, y)$

D:  $\frac{\partial u}{\partial x} = c^2 \frac{\partial u}{\partial y}$

Correct Answer: Option-B

Question97: Value of the Beta function at  $(1/2, 1/2)$  is

A:  $\beta(1/2, 1/2) = \pi$

B:  $\beta(1/2, 1/2) = \sqrt{\pi}$

C:  $\beta(1/2, 1/2) = \frac{\pi}{2}$

D:  $\beta(1/2, 1/2) = 1$

Correct Answer: Option-A

Question98: Value of the Riemann Zeta function  $\zeta(s)$  at  $s = 2$  is

A:  $\zeta(2) = 1$

B:  $\zeta(2) = 2!$

C:  $\zeta(2) = \pi/2$

D:  $\zeta(2) = \frac{\pi^2}{6}$

Correct Answer: Option-D

Question99: Let  $\bar{T}, \bar{N}, \bar{B}$  and  $k$  be unit tangent vector, principal unit normal vector, binormal vector and curvature respectively. Then

A:  $\bar{B} = \bar{T} \times \bar{N}$

B:  $\bar{B} = \frac{1}{k} \frac{d\bar{T}}{ds}$

C:  $\bar{B} = \frac{d\bar{N}}{dt}$

D:  $\bar{B} = \frac{d\bar{N}}{ds} \times \frac{d\bar{T}}{ds}$

Correct Answer: Option-A

Question100: Let A and B be fuzzy subsets of a crisp set X. If  $\mu_A(x)$  and  $\mu_B(x)$  are the membership value of x in A and B respectively, then which of the following gives a membership value of x in  $A \cap B$

A:  $\max\{\mu_A(x), \mu_B(x)\}$

B:  $\mu_A(x) + \mu_B(x) - \mu_A(x)\mu_B(x)$

C:  $\min\{\mu_A(x), \mu_B(x)\}$

D:  $1 - \mu_A(x)\mu_B(x)$

Correct Answer:- Option-C